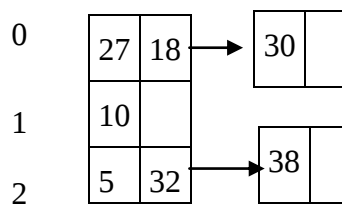


1)



$$38(\text{mod}3) = 2$$

1

2) Table for mod(key, 17)

10	01010
20	00011
3	00011
7	00111
13	01101
14	01110
18	00001
21	00100
25	01000
16	10000
38	00100
30	01101
37	00011
35	00001
23	00110

Bkfr = 3

0			
1			

Desired Lf = 2/3

bv = 0, h = 1

Add 10

0	10		
1			

$bv = 0, h = 1, \quad 1/6 \neq \text{Desired Lf}$

Add 20, 3

0	10		
1	20	3	

$bv = 0, h = 1, \quad 3/6 = 1/2 \neq \text{Desired Lf}$

Add 7

0	10		
1	20	3	7

$bv=0, h=1 \quad 4/6 = 2/3 = \text{Desired Lf} \rightarrow \text{Add 2 records and update}$

Add 13, 14

0	10	14	
1	20	3	7

$\rightarrow$

13		
----	--	--

Update

00			
1	20	3	7
10	10	14	

$\rightarrow$

13		
----	--	--

$bv = 1 \quad h = 1$

$6 / 9 = 2/3 = \text{Desired Lf} \rightarrow \text{Add 2 records and update}$

Add 18, 21

00	21		
1	20	3	7
10	10	14	

→

13	18	
----	----	--

Update

00	21		
01	13	18	
10	10	14	
11	20	3	7

$bv = 2, h = 1 \rightarrow bv = 2^h \rightarrow bv = 0, h = 2$

$8 / 12 = 2/3 = \text{Desired Lf} \rightarrow \text{Add 2 records and update}$

Add 25, 16

00	21	25	16
01	13	18	
10	10	14	
11	20	3	7

 $bv = 0, h = 2$

Update

000	25	16	
01	13	18	
10	10	14	
11	20	3	7
100	21		

$bv = 1, h = 2$

$10/15 = 2/3 = \text{Desired Lf} \rightarrow \text{Add 2 records and update}$

Add 38, 30

000	25	16	
01	13	18	30
10	10	14	
11	20	3	7
100	21	38	

Update

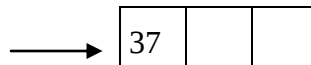
000	25	16	
001	18		
10	10	14	
11	20	3	7
100	21	38	
101	13	30	

bv = 2, h = 2

$12/18 = 2/3 = \text{Desired Lf} \rightarrow \text{Add 2 records and update}$

Add 37, 35

000	25	16	
001	18	35	
10	10	14	
11	20	3	7
100	21	38	
101	13	30	



Update

000	25	16	
001	18	35	
010	10		
11	20	3	7
100	21	38	
101	13	30	
110	14		

→

37		
----	--	--

bv = 3, h=2 $14/21 = 2/3 = \text{Desired Lf} \rightarrow \text{Add 2 records and update}$

Add 23

000	25	16	
001	18	35	
010	10		
11	20	3	7
100	21	38	
101	13	30	
110	14	23	

→

37		
----	--	--

bv = 3, h=2

Another record is necessary before an update operation.

3) a) $2^h - bv = 13$ blocks hashed at level $h = 4$

b) $2 \cdot bv = 6$ blocks hashed at level $h + 1 = 5$

c) 10010 is the address of the last bucket of the file

d) 1111 is the address of the last bucket of the file hashed at h

e) $\text{mod}(54, 37) = 17 = 10001 \text{ b}$

$0001 < bv \rightarrow$ the following bit is taken which is 1

now the pseudo key equals to 10001 b.

The number of bucket which contains 54 is 10001.

4) a) $1024 - 200 = 824$ blocks hashed at level $h = 10$

b) $200 \times 2 = 400$ blocks hashed at level $h+1 = 5$

c) 10011000111 is the address of the last bucket in the file.

d) 11111 11111 is the address of the last bucket of the file hashed at level 10.

e) $\text{mod}(5178, 2039) = 1100 \text{ d} = 10001001100 \text{ b}$

$00010 \ 01100 < bv$, so the following bit is taken which is 1.

Then, the pseudo key is 10001001100.¹

¹ Solutions are due to Sefa Şahin Koç (Övünç Sezer hw is used for double checking).