

Filters (cont.)

CS 554 – Computer Vision

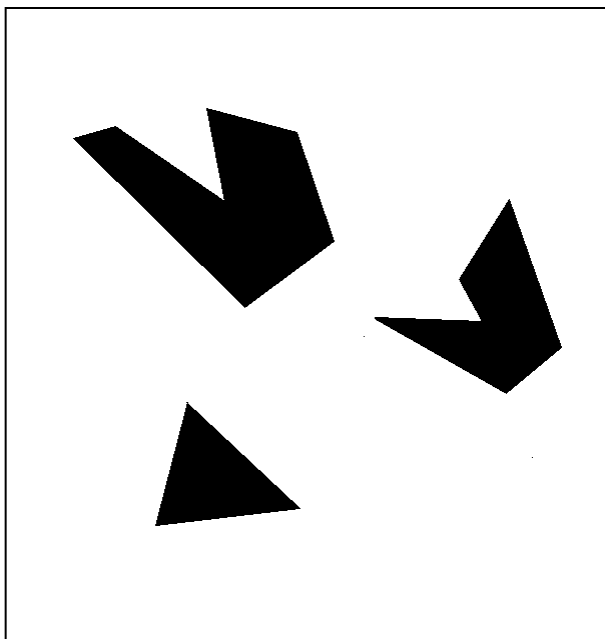
Pinar Duygulu

Bilkent University

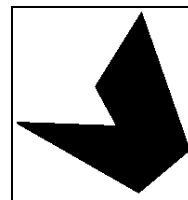
Today's topics

- Image Formation
- Image filters in spatial domain
 - Filter is a mathematical operation of a grid of numbers
 - Smoothing, sharpening, measuring texture
- Image filters in the frequency domain
 - Filtering is a way to modify the frequencies of images
 - Denoising, sampling, image compression
- Templates and Image Pyramids
 - Filtering is a way to match a template to the image
 - Detection, coarse-to-fine registration

Template matching



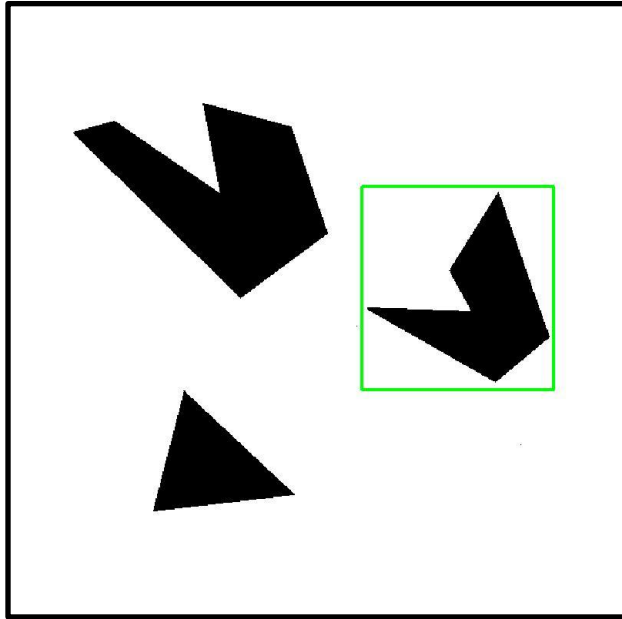
Scene



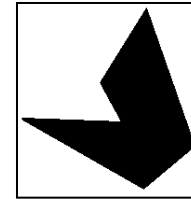
Template (mask)

A toy example

Template matching

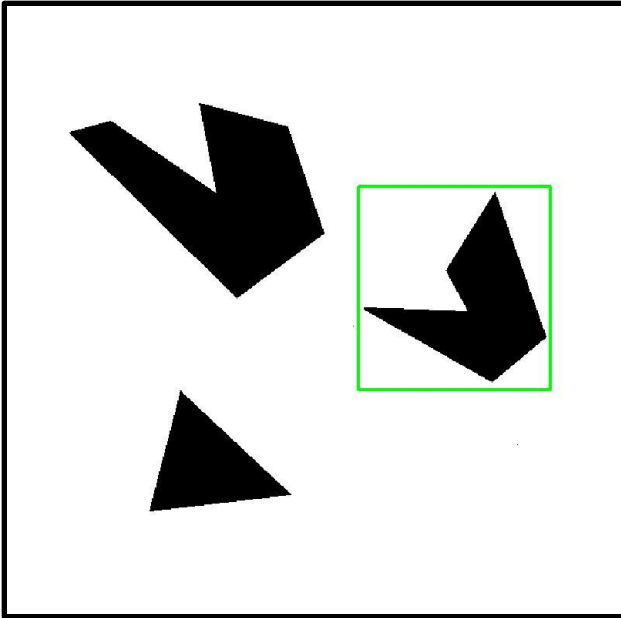


Detected template

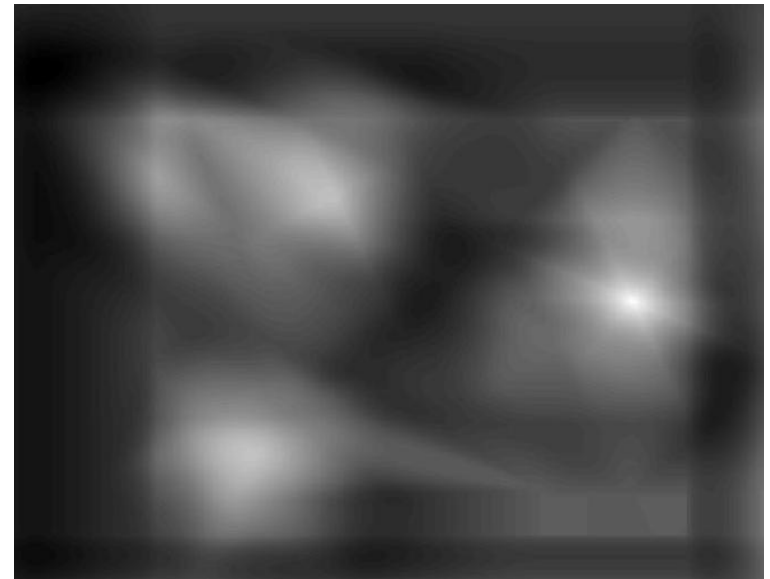


Template

Template matching



Detected template



Correlation map

Where's Waldo?

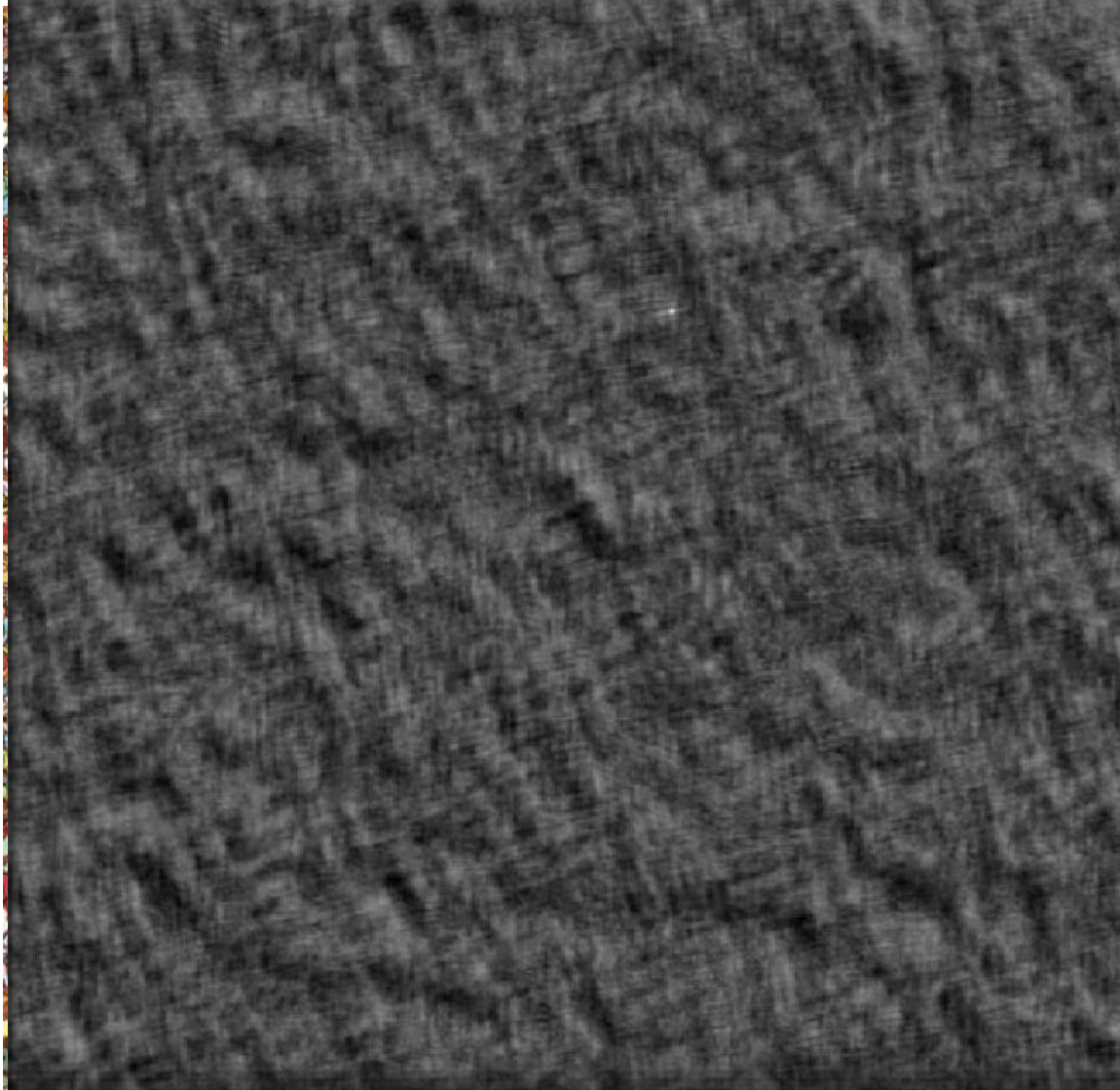


Scene



Template

Where's Waldo?



Scene

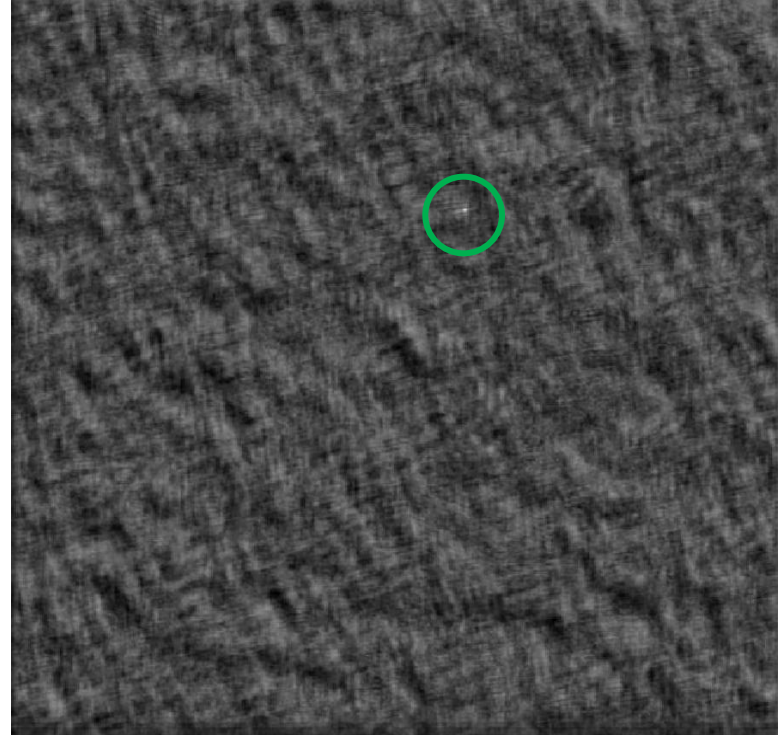


Template

Where's Waldo?



Detected template



Correlation map

Template matching



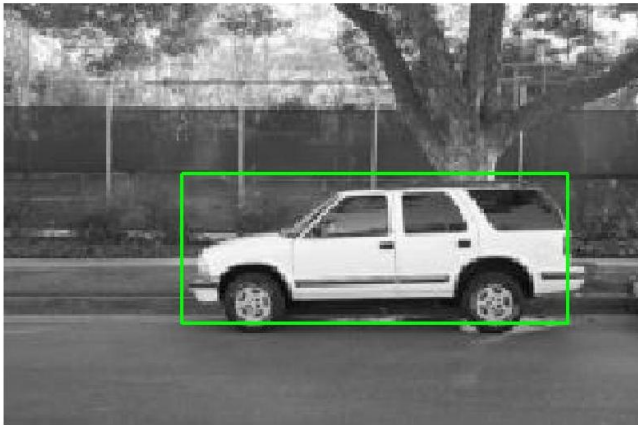
Scene



Template

What if the template is not identical to some subimage in the scene?

Template matching



Detected template



Template

Match can be meaningful, if scale, orientation, and general appearance is right.

Application

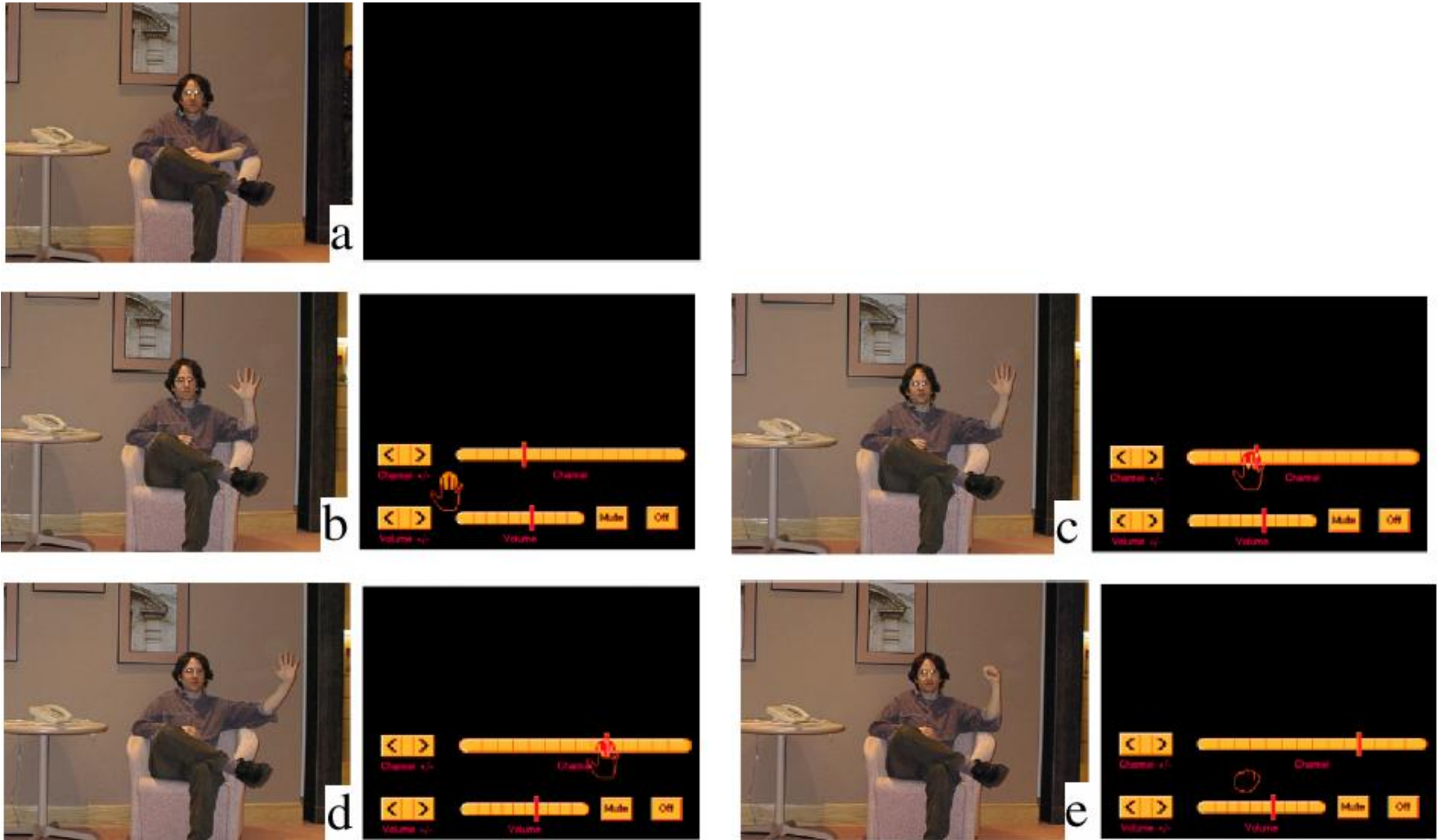

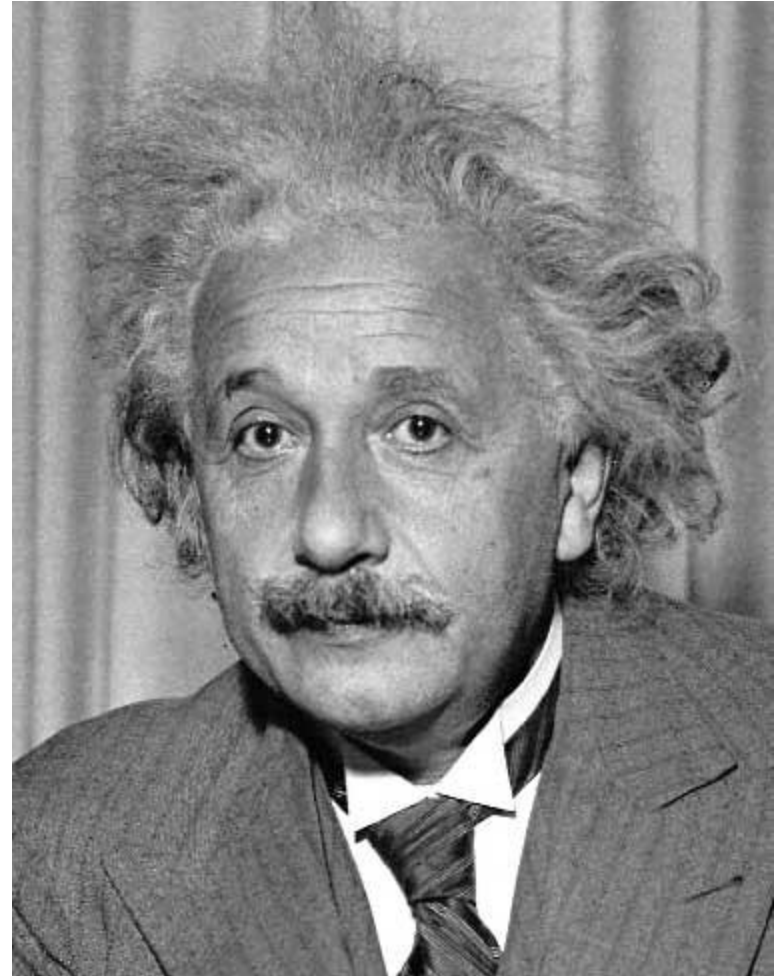


Figure from "Computer Vision for Interactive Computer Graphics," W.Freeman et al, IEEE Computer Graphics and Applications, 1998
copyright 1998, IEEE

Template matching

- Goal: find  in image
- Main challenge: What is a good similarity or distance measure between two patches?
 - Correlation
 - Zero-mean correlation
 - Sum Square Difference
 - Normalized Cross Correlation

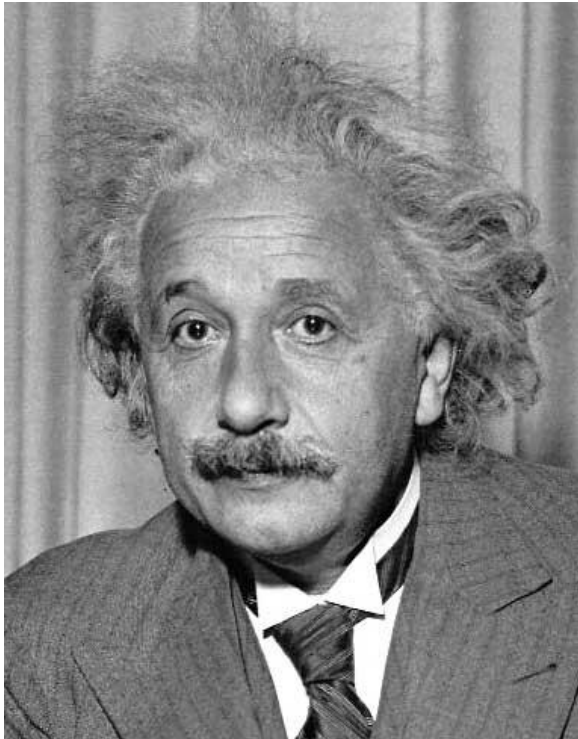


Matching with filters

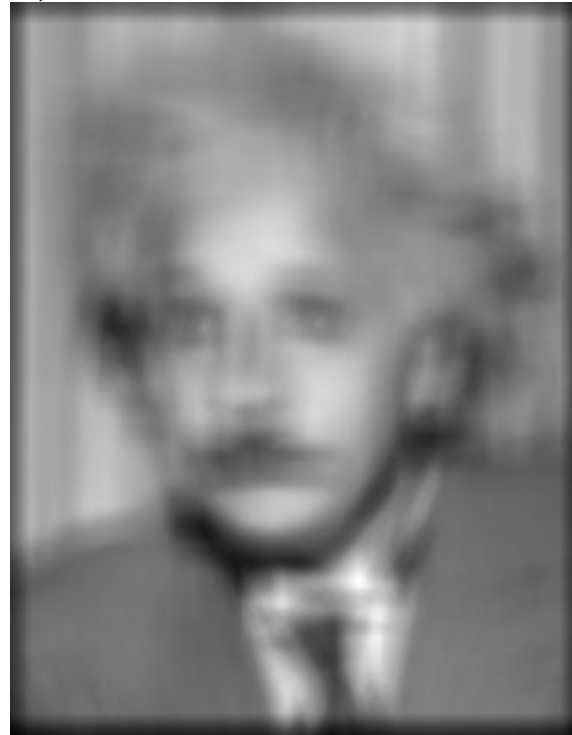
- Goal: find  in image
- Method 0: filter the image with eye patch

$$h[m,n] = \sum_{k,l} g[k,l] f[m+k,n+l]$$

f = image
g = filter



Input



Filtered Image

What went wrong?

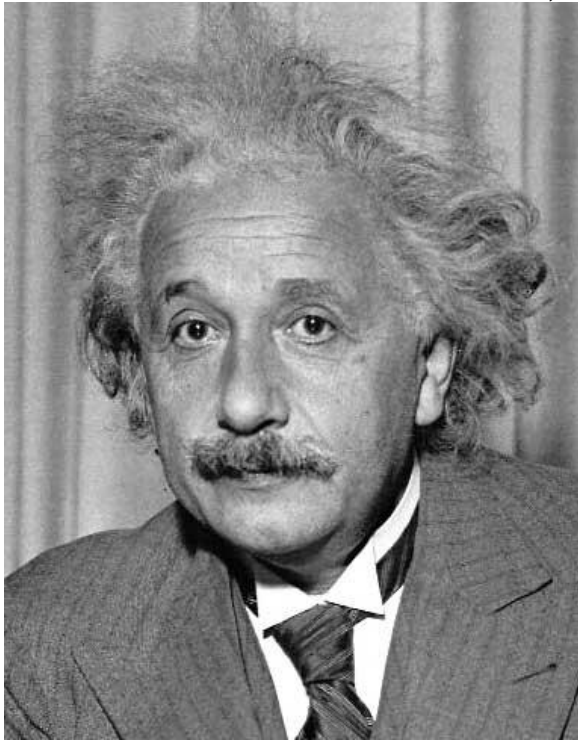
response is stronger
for higher intensity

Matching with filters

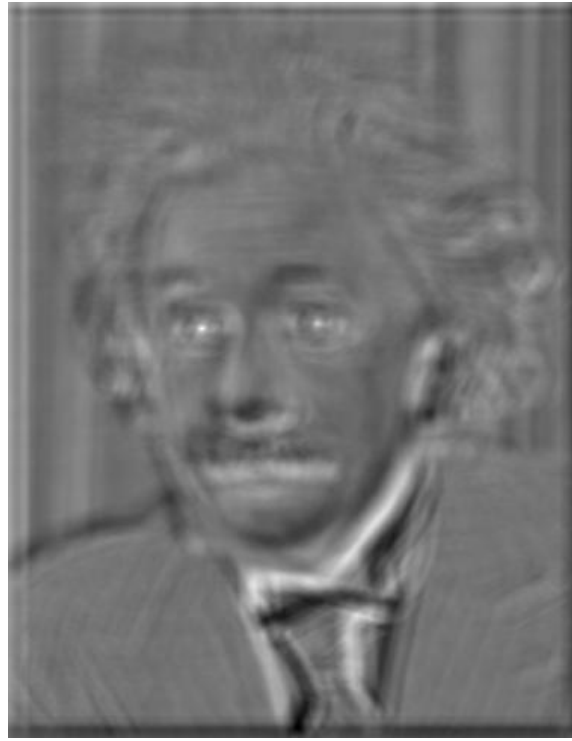
- Goal: find  in image
- Method 1: filter the image with zero-mean eye

$$h[m,n] = \sum_{k,l} (f[k,l] - \bar{f})(g[m+k, n+l])$$

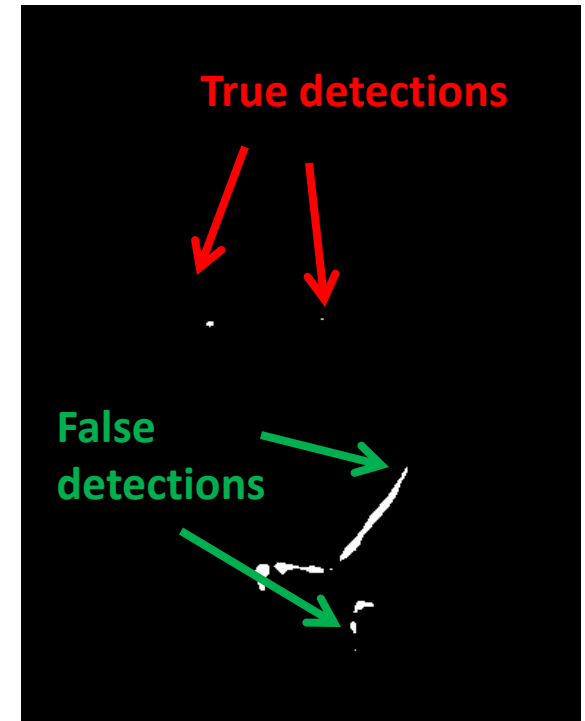
\bar{f} ← mean of f



Input




Filtered Image (scaled)

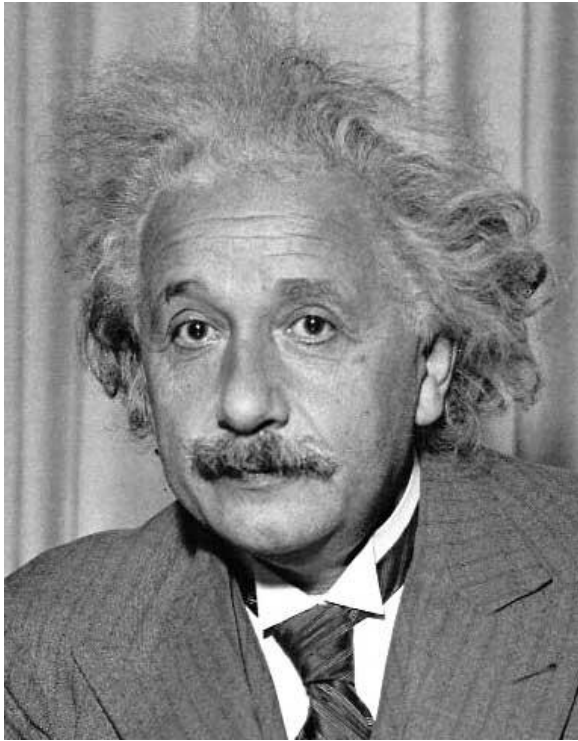


Thresholded Image

Matching with filters

- Goal: find  in image
- Method 2: SSD

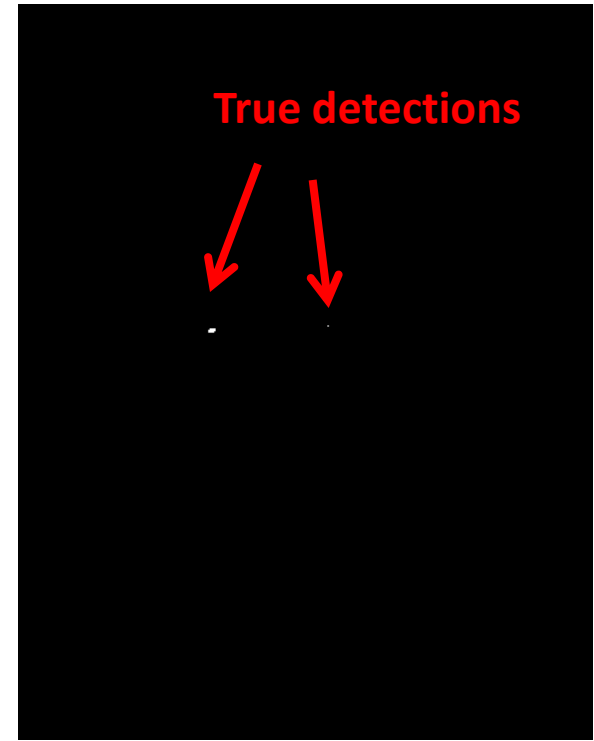
$$h[m,n] = \sum_{k,l} (g[k,l] - f[m+k,n+l])^2$$



Input



1- sqrt(SSD)

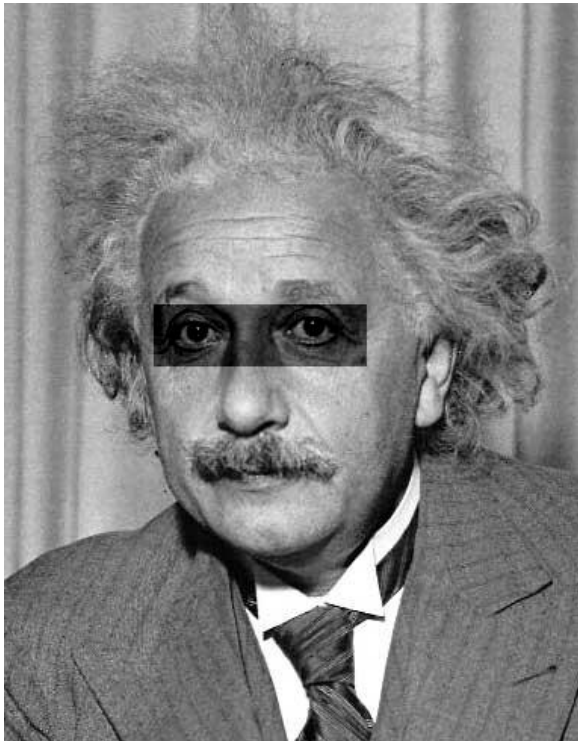


Thresholded Image

Matching with filters

- Goal: find  in image
- Method 2: SSD

$$h[m,n] = \sum_{k,l} (g[k,l] - f[m+k,n+l])^2$$



Input




1- sqrt(SSD)

What's the potential downside of SSD?

SSD is sensitive to average intensity


Matching with filters

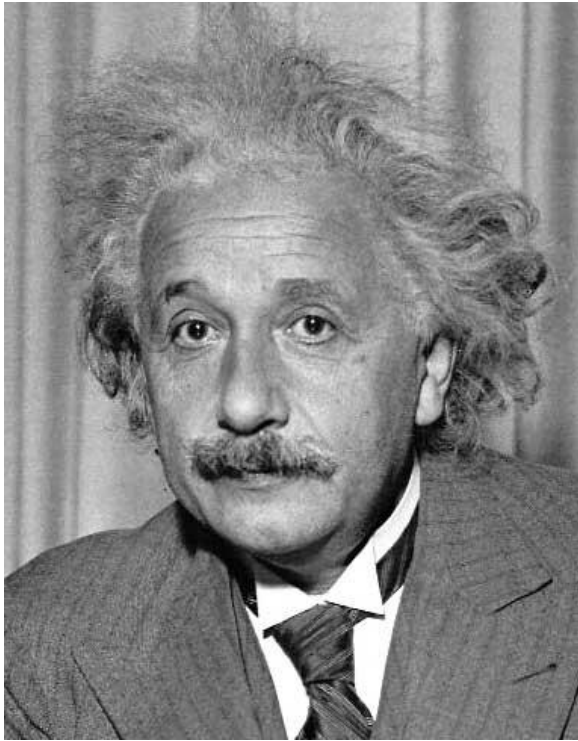
- Goal: find  in image
- Method 3: Normalized cross-correlation

$$h[m,n] = \frac{\sum_{k,l} (g[k,l] - \overset{\text{mean template}}{\bar{g}})(f[m-k,n-l] - \overset{\text{mean image patch}}{\bar{f}_{m,n}})}{\left(\sum_{k,l} (g[k,l] - \bar{g})^2 \sum_{k,l} (f[m-k,n-l] - \bar{f}_{m,n})^2 \right)^{0.5}}$$

Matlab: `normxcorr2(template, im)`

Matching with filters

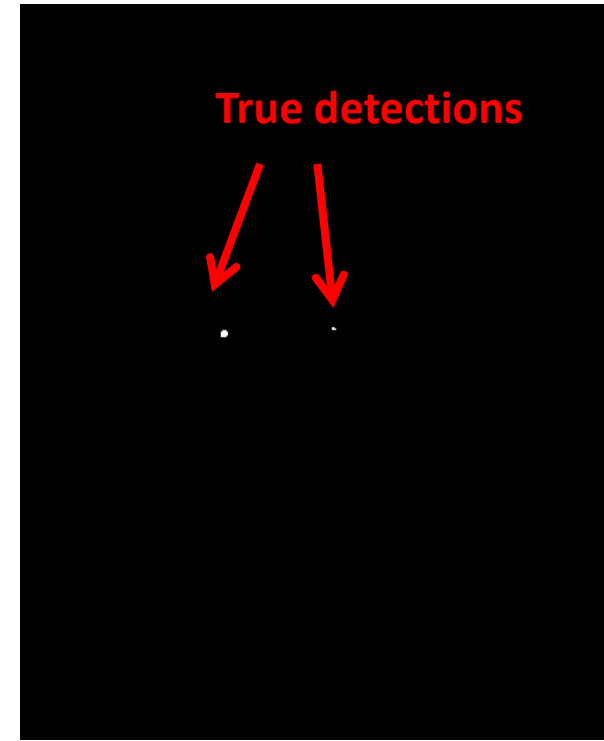
- Goal: find  in image
- Method 3: Normalized cross-correlation



Input




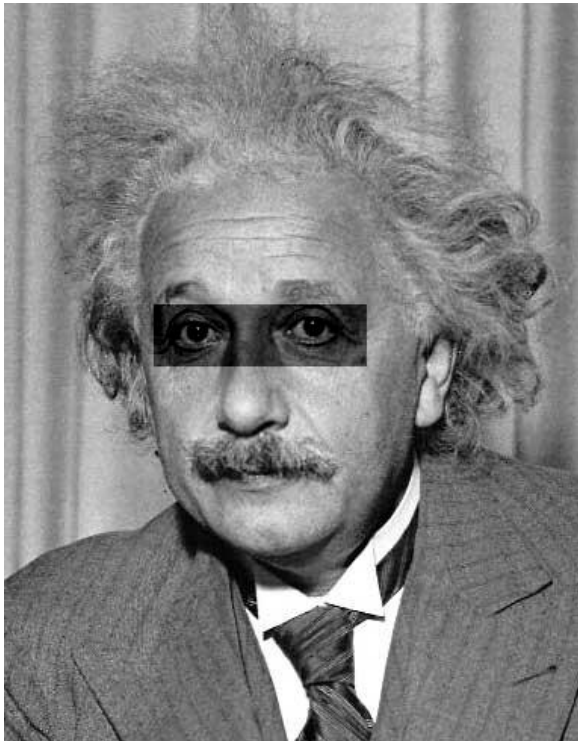
Normalized X-Correlation



Thresholded Image

Matching with filters

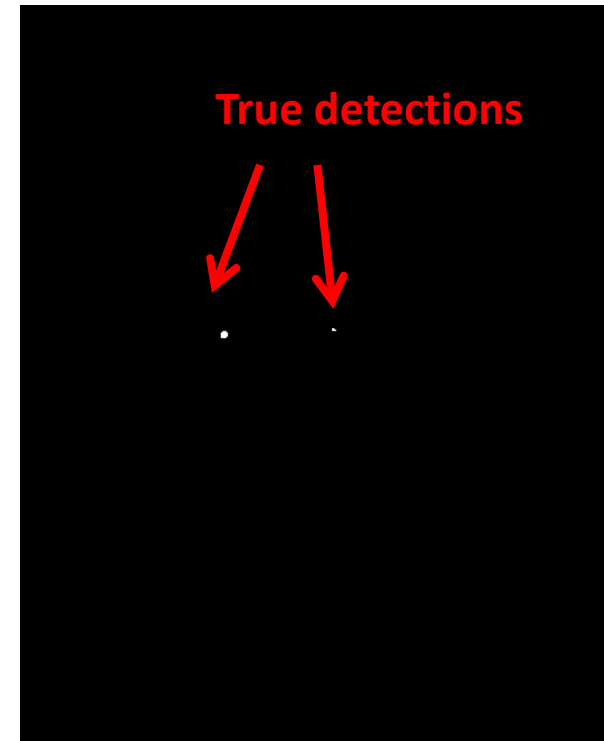
- Goal: find  in image
- Method 3: Normalized cross-correlation



Input



Normalized X-Correlation



Thresholded Image

Q: What is the best method to use?

A: Depends

- SSD: faster, sensitive to overall intensity
- Normalized cross-correlation: slower, invariant to local average intensity and contrast

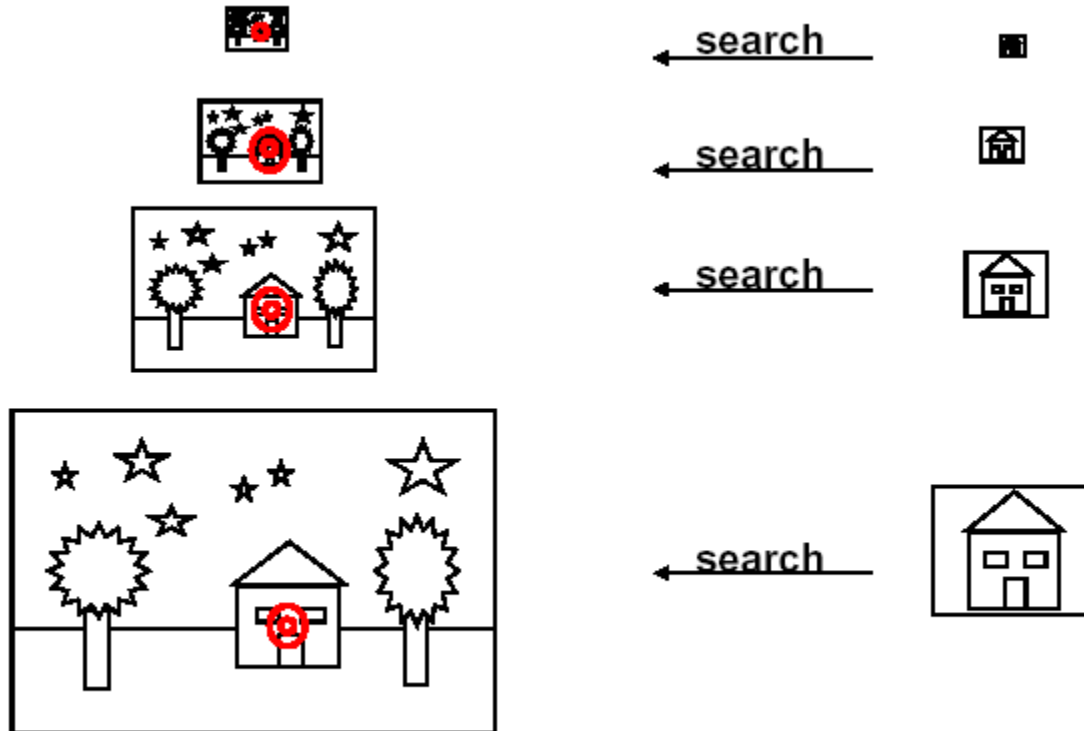
Q: What if we want to find larger or smaller eyes?

Motivation for studying scale.



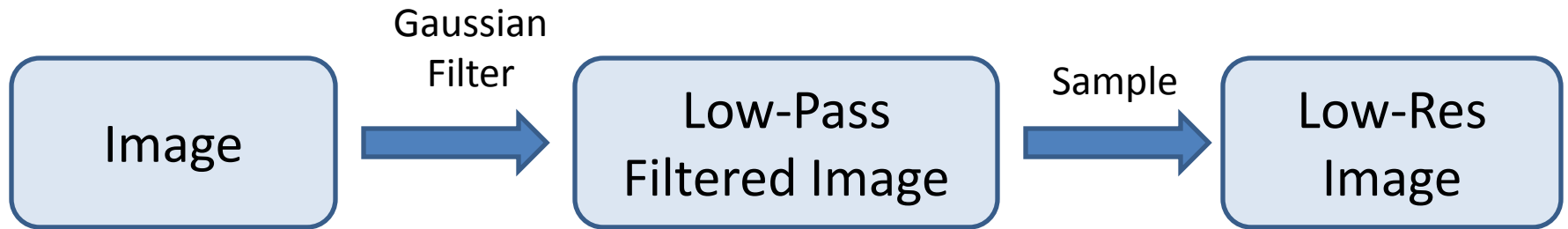
ELDER AND ZUCKER: LOCAL SCALE CONTROL FOR EDGE DETECTION AND BLUR ESTIMATION

A: Image Pyramid

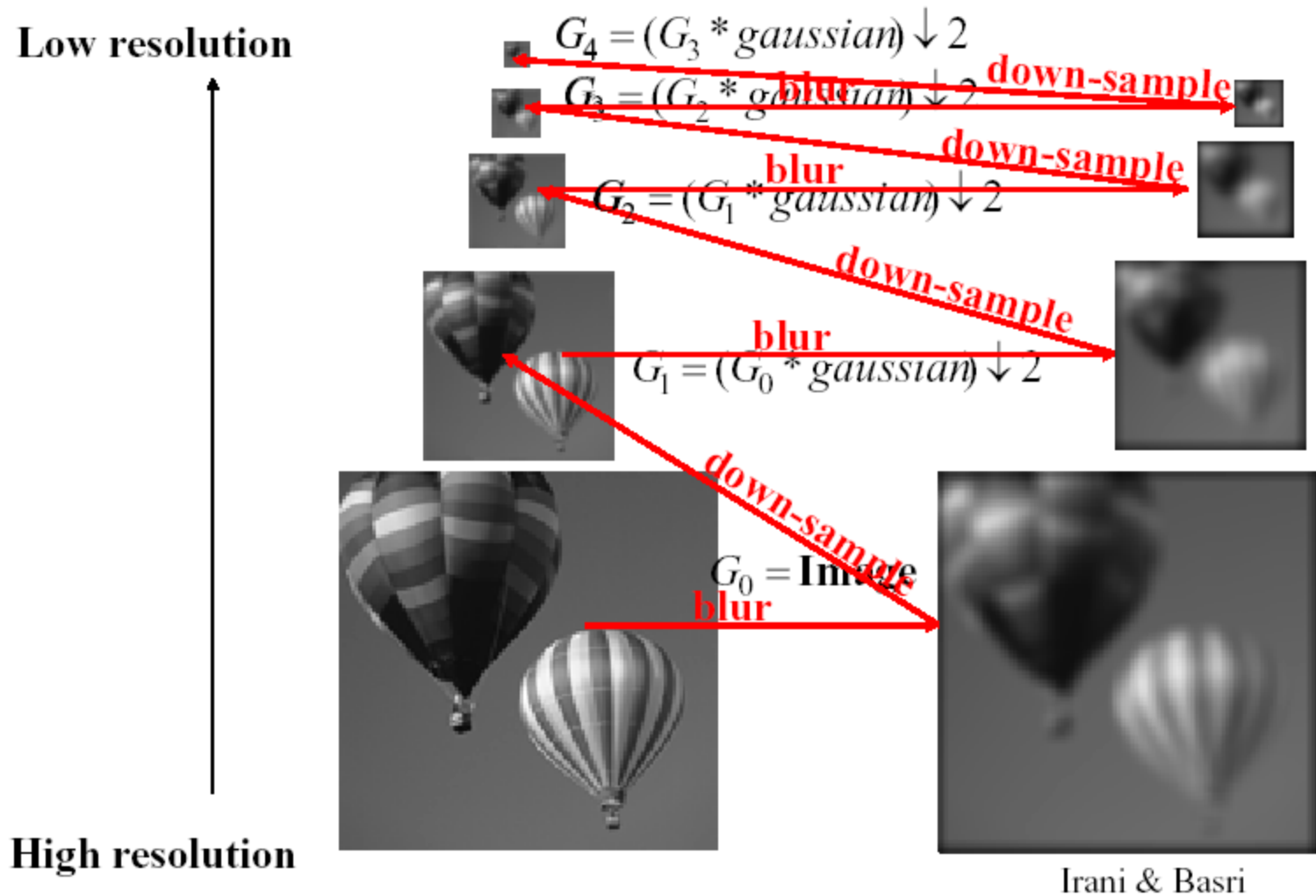


Irani & Basri

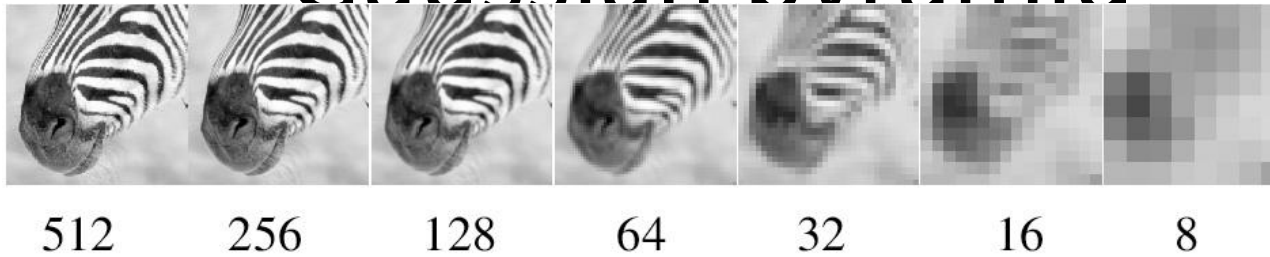
Review of Sampling



Gaussian Pyramid



Gaussian pyramid



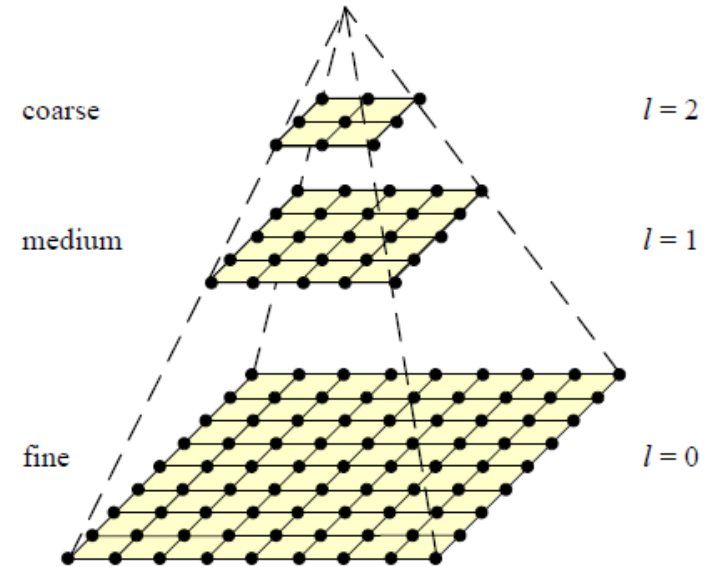
Template Matching with Image Pyramids

Input: Image, Template

1. Match template at current scale
2. Downsample image
3. Repeat 1-2 until image is very small
4. Take responses above some threshold, perhaps with non-maxima suppression

Coarse-to-fine Image Registration

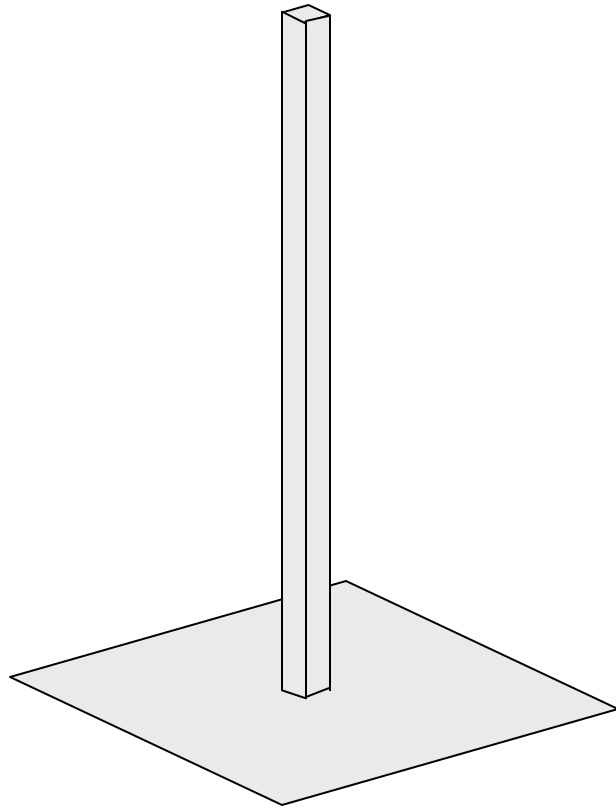
1. Compute Gaussian pyramid
2. Align with coarse pyramid
3. Successively align with finer pyramids
 - Search smaller range



Why is this faster?

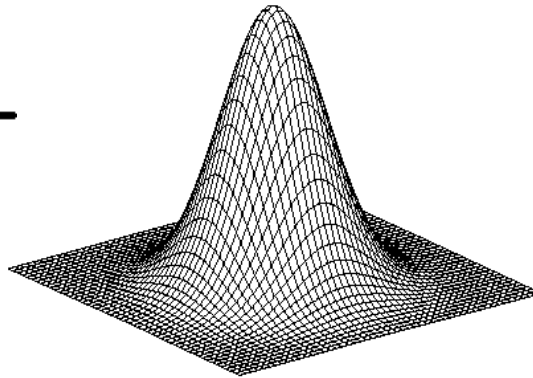
Are we guaranteed to get the same result?

Laplacian filter



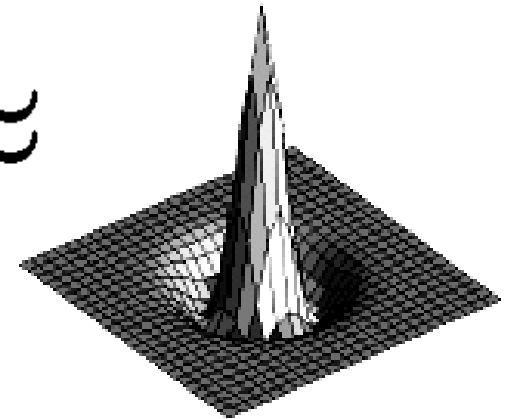
unit impulse

—



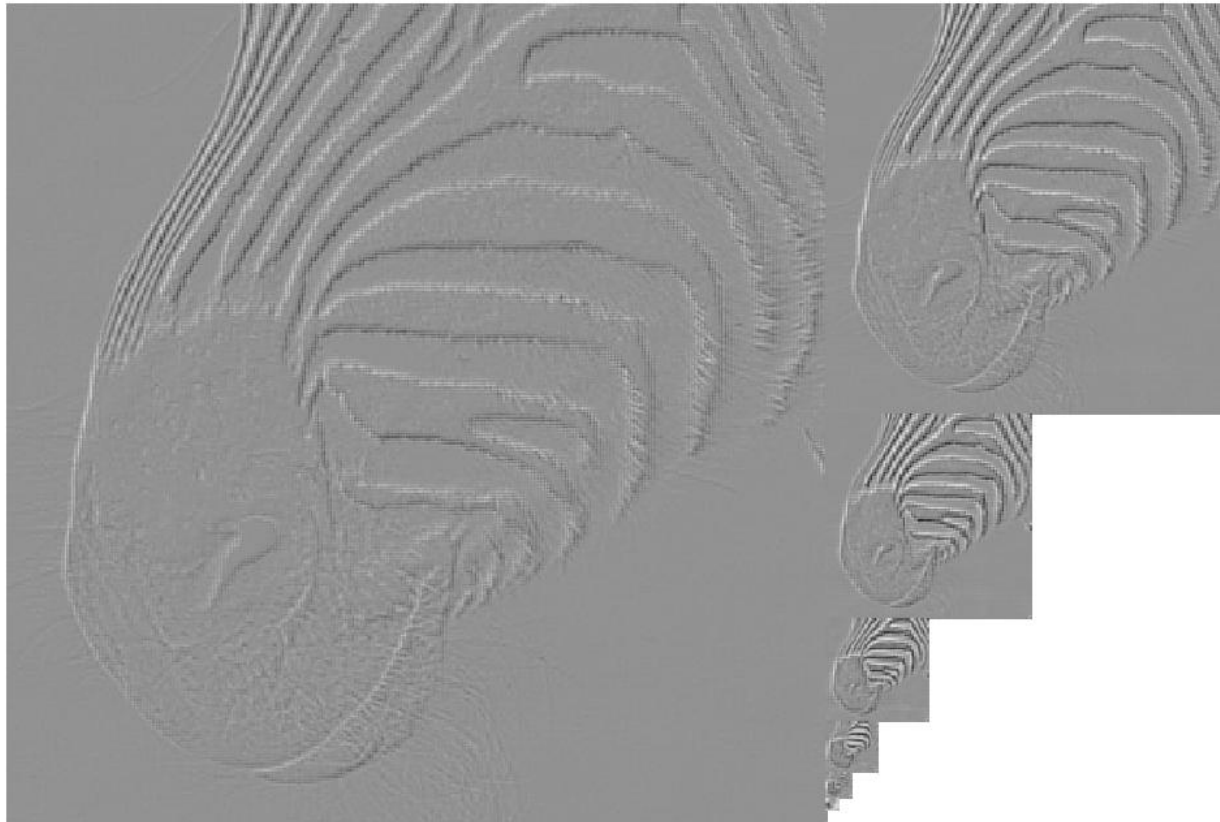
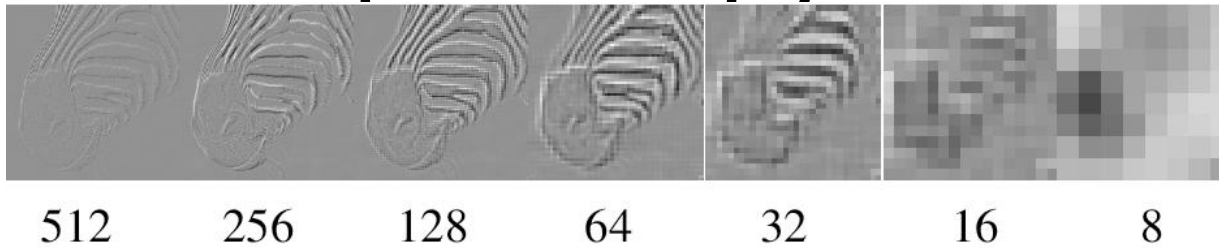
Gaussian

\approx

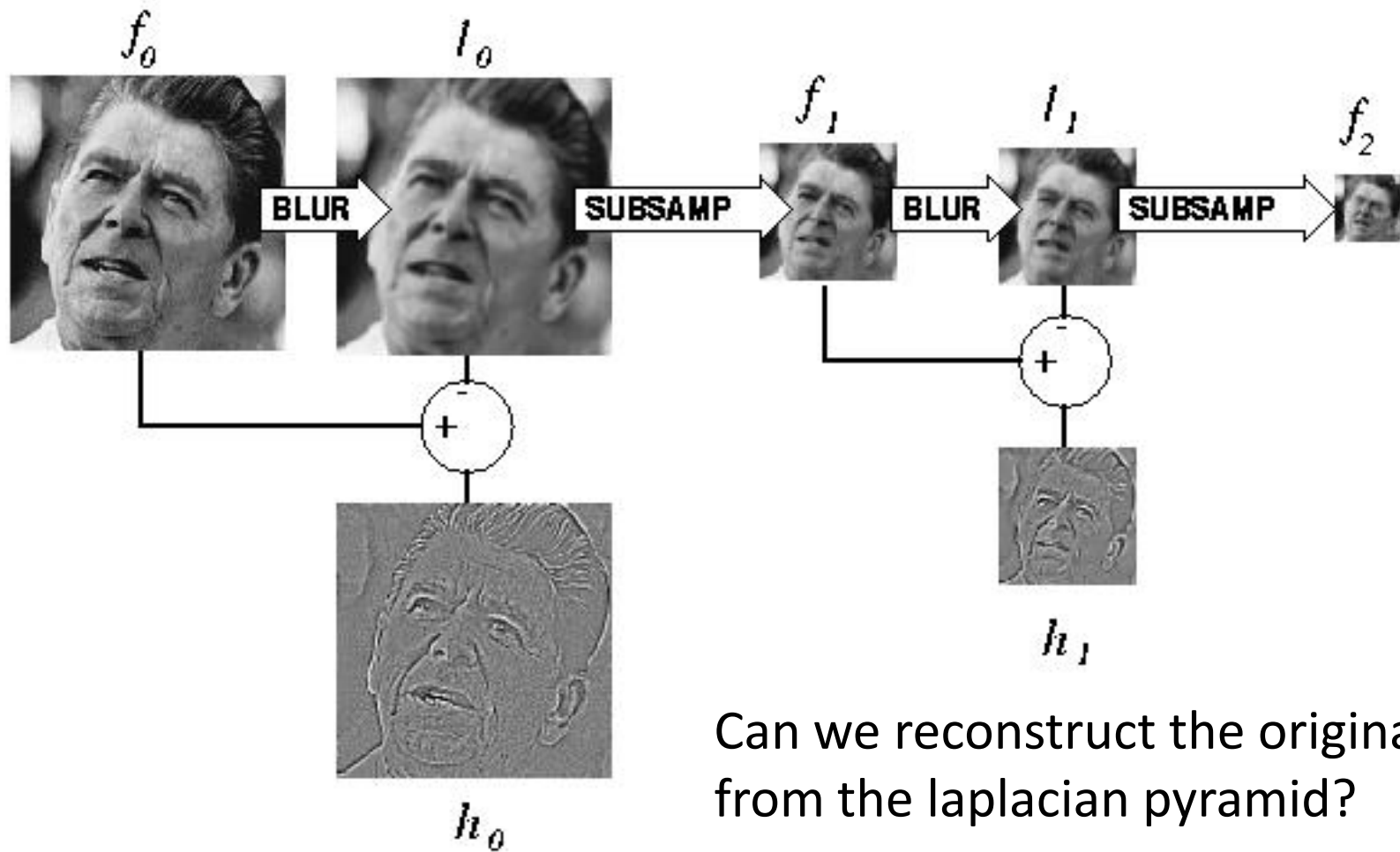


Laplacian of Gaussian

Laplacian pyramid

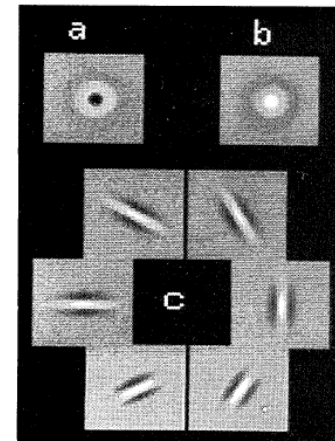
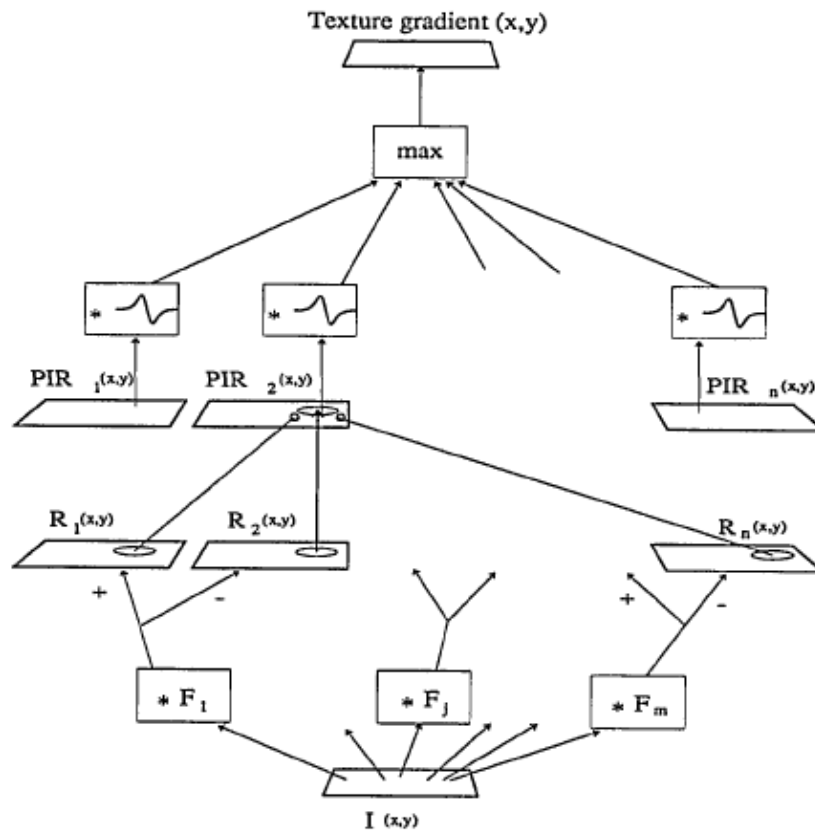


Computing Gaussian/Laplacian Pyramid



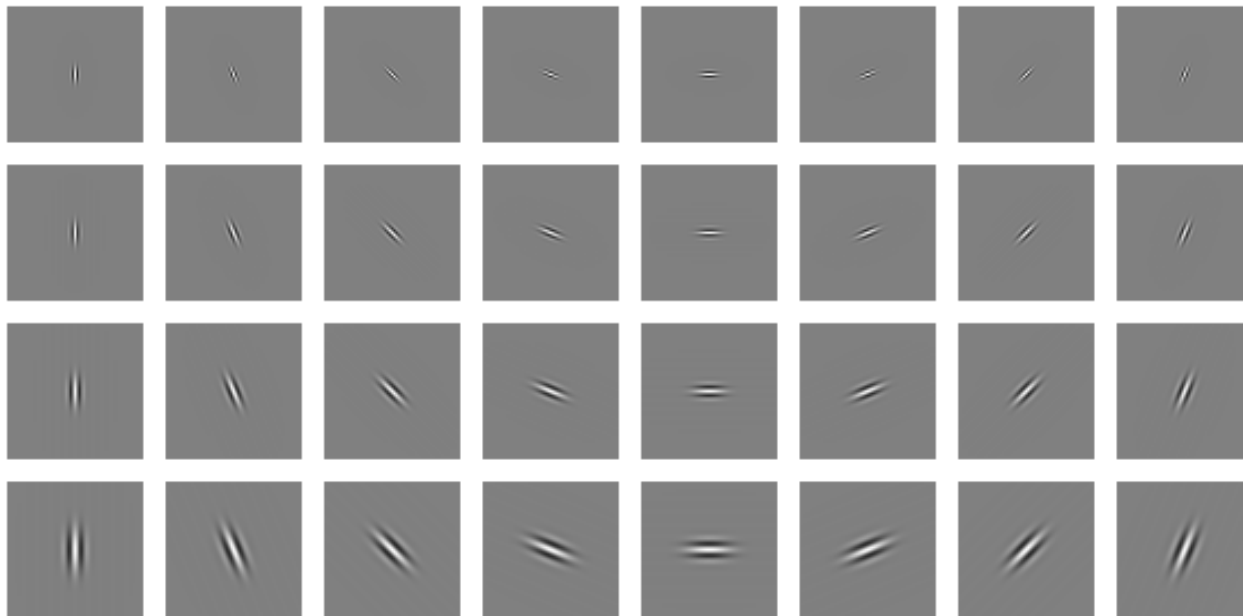
Can we reconstruct the original from the laplacian pyramid?

Texture segmentation



Clues from Human Perception

- Early processing in humans filters for various orientations and scales of frequency
- Perceptual cues in the mid-high frequencies dominate perception
- When we see an image from far away, we are effectively subsampling it



Early Visual Processing: Multi-scale edge and blob filters