PART 1:
Implement the k-means algorithm to cluster the image pixels. Your algorithm should take the pixels of an RGB image, group the pixels into k clusters, and output the clustering vectors as well as the labels of the clustered pixels. In the RGB space, each pixel is represented with 3 values, which are in between 0 and 255.

To test your algorithm, use the image (sample.jpg) provided on the course website. First run your implementation for the following values of k = {2, 3, 4, 5, 6, 7}. For each of these k values,

- Report the clustering error
- Give the values of the clustering vectors
- Give the clustered image. To obtain this clustered image, represent each pixel with the RGB values of its clustering vector.

Then, using your implementation, determine the optimum k value for this image. For that, do NOT just consider the k values given above (i.e., do NOT just consider k = {2, 3, 4, 5, 6, 7}). Explain how you determine the optimum value. Moreover, for your optimum k value, report the clustering error and give the clustered image, as explained above.

In your report, give all details of your implementation, such as how to select the initial values and the stopping criterion. Your report should also include the aforementioned outputs. Since the outputs include the clustered images, submit a color printout of your report.

In this assignment, you may use any programming language you would like. If you do not know how to process images in your preferred programming language, you can employ the following Matlab codes. Of course, if you do not want to use the following codes, that is completely ok as long as you process the image pixels and give the required outputs.

```matlab
% Reads sample.jpg into an im matrix, whose dimensions are N, M, and 3
im = imread('sample.jpg');

% Reshapes the 3D im matrix into a 2D matrix, called im2, whose
% dimensions are NxM and 3. In this 2D matrix, each row corresponds to
% a pixel, and the columns correspond to red, green, and blue channels
% in the RGB color space, respectively
im2 = reshape(im,[size(im,1)*size(im,2) 3]);

% You need to run the k-means algorithm on the im2 matrix. Your
% k-means algorithm should output the clustering vectors (let’s call
% them V) and the labels of the clustered pixels (let’s call them cmap).
% To implement the k-means algorithm, you can use Matlab. Of course, you
% have to write your own code; you cannot use the kmeans built-in
% function of Matlab. However, if you find Matlab too slow (and if you
% do not know how to read images in your preferred programming
% language), you can write the contents of im2 into a file and read this
% file in your program. Similarly, you can calculate clustering vectors
% V and labels cmap in your program, write them into files, and read
% them from Matlab to obtain the clustered image.
```
% Suppose that your program outputs matrix V, whose dimensions are k 
% and 3, and vector cmap, whose dimension is NxM. Also suppose that 
% your labels are in between 1 and k. Then you may use the following 
% Matlab codes to produce the clustered image 
cmap2 = reshape(cmap,[size(im,1) size(im,2)]); 
M = V / 255; 
clusteredImage = label2rgb(cmap2, M); 

% Shows the clustered image in Matlab and writes it into a bitmap file 
figure, imshow(clusteredImage) 
imwrite(clusteredImage,'output.bmp')

PART 2:

Implement an agglomerative hierarchical clustering algorithm to cluster the image pixels. Similarly, your 
algorithm should take the pixels of an RGB image, group the pixels into k clusters using this 
agglomerative algorithm, and output the clustering vectors as well as the labels of the clustered pixels.

The computational time of this part could be high due to the number of pixels in the image. Thus, 
propose a technique to overcome this problem. For example, you may “somehow” form small groups of 
pixels and consider each of these groups as the initial clusters of your agglomerative algorithm. 
However, downsampling an image into a lower resolution and running your algorithm on this 
downsampled image will NOT be accepted as a solution. Do not forget that there is not only one 
correct solution for this part. Thus, try to consider different alternatives.

Test your algorithm on the same image (sample.jpg) and obtain the results for different values of k. 
Prepare a report for this second part similar to Part 1, also addressing the same questions given in the 
first part. Additionally, for this second part, give the details of your technique that you will propose to 
overcome the computational time problem.

WHAT TO SUBMIT:

Prepare your report for the first and the second part as explained above. The last part of your report 
should include a brief comparison of the results that you will obtain in Part 1 and Part 2. Your report 
should be a maximum of 4 pages.

Similar to the first assignment, prepare your report neatly and properly. But this time, since it includes 
the clustered images, submit a color printout of your report.

Also similar to your first assignment, this homework asks you to implement the k-means algorithm and 
an agglomerative hierarchical clustering algorithm by writing your own codes. Thus, you are not 
allowed using any machine learning package. In your implementation, you may use any programming 
language you would like.

Additionally, email the source code of your implementation. The subject line of your email should be CS 
550: HW2. Do not submit the printout of your source code.