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- Edge detection is the process of finding meaningful transitions in an image.
- The points where sharp changes in the brightness occur typically form the border between different objects or scene parts.
- These points can be detected by computing intensity differences in local image regions.
- Initial stages of mammalian vision systems also involve detection of edges and local features.

Sharp changes in the image brightness occur at:

- Object boundaries
  - A light object may lie on a dark background or a dark object may lie on a light background.
- Reflectance changes
  - May have quite different characteristics zebras have stripes, and leopards have spots.
- Cast shadows
- Sharp changes in surface orientation
- Further processing of edges into lines, curves and circular arcs result in useful features for matching and recognition.

- Basic idea: look for a neighborhood with strong signs of change.
- Problems:
  - Neighborhood size
  - How to detect change
- Differential operators:

- 818226248233252581822624
- Attempt to approximate the gradient at a pixel via masks.
- Threshold the gradient to select the edge pixels.

# Edge models



#### abc

**FIGURE 10.8** From left to right, models (ideal representations) of a step, a ramp, and a roof edge, and their corresponding intensity profiles.

**FIGURE 10.9** A  $1508 \times 1970$  image showing (zoomed) actual ramp (bottom, left), step (top, right), and roof edge profiles. The profiles are from dark to light, in the areas indicated by the short line segments shown in the small circles. The ramp and "step" profiles span 9 pixels and 2 pixels, respectively. The base of the roof edge is 3 pixels. (Original image courtesy of Dr. David R. Pickens, Vanderbilt University.)

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Adapted from Gonzales and Woods

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**FIGURE 10.11** First column: Images and intensity profiles of a ramp edge corrupted by random Gaussian noise of zero mean and standard deviations of 0.0, 0.1, 1.0, and 10.0 intensity levels, respectively. Second column: First-derivative images and intensity profiles. Third column: Second-derivative images and intensity profiles.

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- Three fundamental steps in edge detection:
  - 1. Image smoothing: to reduce the effects of noise.
  - 2. Detection of edge points: to find all image points that are potential candidates to become edge points.
  - 3. Edge localization: to select from the candidate edge points only the points that are true members of an edge.

 $mask\ M\ =\ [-1,0,1]$ 

$S_1$			12	12	12	12	12	24	24	24	24	24
$S_1$	$\otimes$	M	0	0	0	0	12	12	0	0	0	0

(a)  $S_1$  is an upward step edge

$S_2$			24	24	24	24	24	12	12	12	12	12
$S_2$	$\otimes$	M	0	0	0	0	-12	-12	0	0	0	0

(b)  $S_2$  is a downward step edge

$S_3$			12	12	12	12	15	18	21	24	24	24
$S_3$	$\otimes$	M	0	0	0	3	6	6	6	3	0	0

(c)  $S_3$  is an upward ramp

$S_4$			12	12	12	12	24	12	12	12	12	12
$S_4$	$\otimes$	M	0	0	0	12	0	-12	0	0	0	0

(d)  $S_4$  is a bright impulse or "line"

Figure 5.11: Cross correlation of four special signals with first derivative edge detecting mask [-1, 0, 1]; (a) upward step edge, (b) downward step edge, (c) upward ramp, and (d) bright impulse. Note that, since the coordinates of **M** sum to zero, output must be zero on a constant region. Adapted from Shapiro and Stockman

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 $\mathbf{mask}\ \mathbf{M}\ =\ [-1,2,-1]$ 

$S_1$			12	12	12	12	12	24	24	24	24	24
$S_1$	$\otimes$	M	0	0	0	0	-12	12	0	0	0	0

(a)  $S_1$  is an upward step edge

$S_2$			24	24	24	24	24	12	12	12	12	12
$S_2$	$\otimes$	M	0	0	0	0	12	-12	0	0	0	0

(b)  $S_2$  is a downward step edge

$S_3$			12	12	12	12	15	18	21	24	24	24
$S_3$	$\otimes$	M	0	0	0	-3	0	0	0	3	0	0

(c)  $S_3$  is an upward ramp

$S_4$			12	12	12	12	24	12	12	12	12	12
$S_4$	$\otimes$	M	0	0	0	-12	24	-12	0	0	0	0

(d)  $S_4$  is a bright impulse or "line"

Figure 5.12: Cross correlation of four special signals with second derivative edge detecting mask  $\mathbf{M} = [-1, 2, -1]$ ; (a) upward step edge, (b) downward step edge, (c) upward ramp, and (d) bright impulse. Since the coordinates of  $\mathbf{M}$  sum to zero, response on constant regions is zero. Note how a *zero-crossing* appears at an output position where different trends in the input signal join. Adapted from Shap

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Adapted from Shapiro and Stockman

## Observations

### Properties of derivative masks:

- Coordinates of derivative masks have opposite signs in order to obtain a high response in signal regions of high contrast.
- The sum of coordinates of derivative masks is zero so that a zero response is obtained on constant regions.
- First derivative masks produce high absolute values at points of high contrast.
- Second derivative masks produce zero-crossings at points of high contrast.

# Smoothing operators for 1D

box smoothing mask M = [1/3, 1/3, 1/3]

[	$S_1$			12	12	12	12	12	24	24	24	24	24
[	$S_1$	$\otimes$	M	12	12	12	12	16	20	24	24	24	24

(a)  $S_1$  is an upward step edge

$S_4$			12	12	12	12	24	12	12	12	12	12
$S_4$	$\otimes$	M	12	12	12	16	16	16	12	12	12	12

(d)  $S_4$  is a bright impulse or "line"

Gaussian smoothing mask M = [1/4, 1/2, 1/4]

$S_1$			12	12	12	12	12	24	24	24	24	24
$S_1$	$\otimes$	M	12	12	12	12	15	21	24	24	24	24

(a)  $S_1$  is an upward step edge

$S_4$			12	12	12	12	24	12	12	12	12	12
$S_4$	$\otimes$	M	12	12	12	15	18	15	12	12	12	12

(d)  $S_4$  is a bright impulse or "line"

Figure 5.13: (Top two rows) Smoothing of step and impulse with box mask [1/3, 1/3, 1/3] (bottom two rows) smoothing of step and impulse with Gaussian mask [1/4, 1/2, 1/4].

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## Observations

Properties of smoothing masks:

- Coordinates of smoothing masks are positive and sum to one so that output on constant regions is the same as the input.
- The amount of smoothing and noise reduction is proportional to the mask size.
- Step edges are blurred in proportion to the mask size.

- Contrast in the 2D picture function f(x, y) can occur in any direction.
- From calculus, we know that the maximum change occurs along the direction of the *gradient*.
- The gradient of an image f(x,y) at location (x,y) is defined as the vector

$$\nabla f = \left[ \frac{\partial f}{\partial x} \ \frac{\partial f}{\partial y} \right]^T.$$

• The magnitude of the gradient

$$|\nabla f| = \left( \left( \frac{\partial f}{\partial x} \right)^2 + \left( \frac{\partial f}{\partial y} \right)^2 \right)^{1/2}$$

gives the maximum rate of increase of f(x, y) per unit distance in the direction of  $\nabla f$ .

• The direction of the gradient

$$\measuredangle(\nabla f) = \tan^{-1}\left(\frac{\partial f}{\partial y} / \frac{\partial f}{\partial x}\right)$$

represents the direction of this change with respect to the x-axis.



Roberts

-1	-1	-1	-1	0	1
0	0	0	-1	0	1
1	1	1	-1	0	1





Sobel

a bc de

fg

#### FIGURE 10.14

A 3  $\times$  3 region of an image (the z's are intensity values) and various masks used to compute the gradient at the point labeled  $z_5$ .



a b c

**FIGURE 10.12** Using the gradient to determine edge strength and direction at a point. Note that the edge is perpendicular to the direction of the gradient vector at the point where the gradient is computed. Each square in the figure represents one pixel.

#### Adapted from Gonzales and Woods

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### original image

### gradient magnitude

### thresholded gradient magnitude

Adapted from Linda Shapiro, U of Washington

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a b c d

**FIGURE 10.16** 

(a) Original image of size  $834 \times 1114$  pixels, with intensity values scaled to the range [0, 1]. (b)  $|g_x|$ , the component of the gradient in the x-direction, obtained using the Sobel mask in Fig. 10.14(f) to filter the image. (c)  $|g_y|$ , obtained using the mask in Fig. 10.14(g). (d) The gradient image,  $|g_x| + |g_y|$ .

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a b c d

FIGURE 10.18

Same sequence as in Fig. 10.16, but with the original image smoothed using a  $5 \times 5$ averaging filter prior to edge detection.

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#### a b

**FIGURE 10.20** (a) Thresholded version of the image in Fig. 10.16(d), with the threshold selected as 33% of the highest value in the image; this threshold was just high enough to eliminate most of the brick edges in the gradient image. (b) Thresholded version of the image in Fig. 10.18(d), obtained using a threshold equal to 33% of the highest value in that image.

- We can smooth the image using a Gaussian filter and then compute the derivative.
- Two convolutions: one to smooth, then another one to differentiate?

 $\rightarrow$  Actually, no - we can use a derivative of Gaussian filter because differentiation is convolution and convolution is associative.

### **Derivative of Gaussian**

# $D_x \otimes (G \otimes I) = (D_x \otimes G) \otimes I$



Adapted from Michael Black, Brown University

### **Derivative of Gaussian**

# $D_x \otimes (G \otimes I) = (D_x \otimes G) \otimes I$



Adapted from Michael Black, Brown University

## **Derivative of Gaussian**

Applying the first derivative of Gaussian



 The Laplacian of a 2D function f(x, y) is a second-order derivative defined as

$$\nabla^2 f = \frac{\partial^2 f}{\partial x^2} + \frac{\partial^2 f}{\partial y^2}.$$

- The Laplacian generally is not used in its original form for edge detection because:
  - It is sensitive to noise.
  - Its magnitude produces double edges.
  - It is unable to detect edge direction.
- However, its zero-crossing property can be used for edge localization.

• 1D Gaussian function:

$$g(x) = \frac{1}{\sqrt{2\pi\sigma}} e^{-\frac{x^2}{2\sigma^2}}.$$

• Derivative of Gaussian (DoG):

$$g'(x) = \frac{-x}{\sigma^2}g(x).$$

• Laplacian of Gaussian (LoG):

$$g''(x) = \left(\frac{x^2}{\sigma^4} - \frac{-1}{\sigma^2}\right)g(x).$$



Figure 5.19: (a) Gaussian g(x) with spread  $\sigma = 2$ ; (b) first derivative g'(x); (c) second derivative g''(x), which looks like the cross section of a sombrero upside down from how it would be worn; (d) all three plots superimposed to show how the extreme slopes of g(x) align with the extremas of g'(x) and the zero crossings of g''(x). Adapted from Sh

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Adapted from Shapiro and Stockman 27



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# Laplacian of Gaussian



Adapted from Gonzales and Woods

# Laplacian of Gaussian

0	0	0	-1	-1	-2	-1	-1	0	0	0
0	0	-2	-4	-8	-9	-8	-4	-2	0	0
0	-2	-7	-15	-22	-23	-22	15	-7	-2	0
-1	-4	-15	-24	-14	-1	-14	-24	-15	-4	-1
-1	-8	-22	-14	52	103	52	-14	-22	-8	-1
-2	-9	-23	-1	103	178	103	-1	-23	-9	-2
-1	-8	-22	-14	52	103	52	-14	-22	-8	-1
-1	-4	-15	-24	-14	-1	-14	-24	-15	-4	-1
0	-2	-7	-15	-22	-23	-22	15	-7	-2	0
0	0	-2	-4	-8	-9	-8	-4	-2	0	0
0	0	0	-1	-1	-2	-1	-1	0	0	0

Figure 5.22: An 11 × 11 mask approximating the Laplacian of a Gaussian with  $\sigma^2 = 2$ . (From Harlalick and Shapiro, Volume I, page 349.)

# Laplacian of Gaussian



sigma=4

LoG zero crossings



Gradient threshold=4



Adapted from David Forsyth, UC Berkeley

Gradient threshold=1



sigma=2

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- Canny defined three objectives for edge detection:
  - 1. Low error rate: All edges should be found and there should be no spurious responses.
  - 2. Edge points should be well localized: The edges located must be as close as possible to the true edges.
  - 3. Single edge point response: The detector should return only one point for each true edge point. That is, the number of local maxima around the true edge should be minimum.

- 1. Smooth the image with a Gaussian filter with spread  $\sigma$ .
- 2. Compute gradient magnitude and direction at each pixel of the smoothed image.
- 3. Zero out any pixel response less than or equal to the two neighboring pixels on either side of it, along the direction of the gradient (non-maxima suppression).
- 4. Track high-magnitude contours using thresholding (hysteresis thresholding).
- 5. Keep only pixels along these contours, so weak little segments go away.

### Non-maxima suppression:

- Gradient direction is used to thin edges by suppressing any pixel response that is not higher than the two neighboring pixels on either side of it along the direction of the gradient.
- This operation can be used with any edge operator when thin boundaries are wanted.



Note: Brighter squares illustrate stronger edge response.

### Hysteresis thresholding:

- Once the gradient magnitudes are thinned, high magnitude contours are tracked.
- In the final aggregation phase, continuous contour segments are sequentially followed.
- Contour following is initiated only on edge pixels where the gradient magnitude meets a high threshold.
- However, once started, a contour may be followed through pixels whose gradient magnitude meet a lower threshold (usually about half of the higher starting threshold).



Very strong edge response. Let's start here

Weaker response but it is connected to a confirmed edge point. Let's keep it.

Continue....

Note: Darker squares illustrate stronger edge response (larger M)

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Adapted from Martial Hebert, CMU 36
1. Compute x and y derivatives of image

$$I_x = G^x_\sigma * I \quad I_y = G^y_\sigma * I$$

2. Compute magnitude of gradient at every pixel

$$M(x,y) = |\nabla I| = \sqrt{I_x^2 + I_y^2}$$

- Eliminate those pixels that are not local maxima of the magnitude in the direction of the gradient
- 4. Hysteresis Thresholding
  - Select the pixels such that M > T<sub>h</sub> (high threshold)

Adapted from Martial Hebert, CMU

• Collect the pixels such that  $M > T_l$  (low threshold) that are neighbors of already collected edge points

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Input image

Adapted from Martial Hebert, CMU



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a b c d

**FIGURE 10.25** (a) Original image of size  $834 \times 1114$ pixels, with intensity values scaled to the range [0, 1]. (b) Thresholded gradient of smoothed image. (c) Image obtained using the Marr-Hildreth algorithm. (d) Image obtained using the Canny algorithm. Note the significant improvement of the Canny image compared to the other two.

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a b c d

**FIGURE 10.26** 

(a) Original head CT image of size  $512 \times 512$  pixels, with intensity values scaled to the range [0, 1]. (b) Thresholded gradient of smoothed image. (c) Image obtained using the Marr-Hildreth algorithm. (d) Image obtained using the Canny algorithm. (Original image courtesy of Dr. David R. Pickens, Vanderbilt University.)

- The Canny operator gives single-pixel-wide images with good continuation between adjacent pixels.
- It is the most widely used edge operator today; no one has done better since it came out in the late 80s. Many implementations are available.
- It is very sensitive to its parameters, which need to be adjusted for different application domains.

# Edge linking

- Hough transform
  - Finding line segments
  - Finding circles
- Model fitting
  - Fitting line segments
  - Fitting ellipses
- Edge tracking

## Hough transform

- The Hough transform is a method for detecting lines or curves specified by a parametric function.
- If the parameters are p<sub>1</sub>, p<sub>2</sub>, ... p<sub>n</sub>, then the Hough procedure uses an n-dimensional accumulator array in which it accumulates votes for the correct parameters of the lines or curves found on the image.





Connection between image (x,y) and Hough (m,b) spaces

- A line in the image corresponds to a point in Hough space
- To go from image space to Hough space:
  - given a set of points (x,y), find all (m,b) such that y = mx + b



Connection between image (x,y) and Hough (m,b) spaces

- A line in the image corresponds to a point in Hough space
- To go from image space to Hough space:
  - given a set of points (x,y), find all (m,b) such that y = mx + b
- What does a point (x<sub>0</sub>, y<sub>0</sub>) in the image space map to?
  - A: the solutions of  $b = -x_0m + y_0$
  - this is a line in Hough space

Adapted from Steve Seitz, U of Washington



- y = mx + b is not suitable (why?)
- The equation generally used is:

 $d = r \sin(\theta) + c \cos(\theta).$ 



```
Accumulate the straight line segments in grav-tone image S to accumulator A.
S[\mathbf{R}, \mathbf{C}] is the input grav-tone image.
NLINES is the number of rows in the image.
NPIXELS is the number of pixels per row.
A[DQ, THETAQ] is the accumulator array.
DQ is the quantized distance from a line to the origin.
THETAQ is the quantized angle of the normal to the line.
     procedure accumulate_lines(S,A);
     A := 0:
     PTLIST := NIL;
     for R := 1 to NLINES
       for C := 1 to NPIXELS
         DR := row_gradient(S,R,C);
         DC := col_gradient(S,R,C);
         GMAG := gradient(DR, DC);
         if GMAG > gradient_threshold
            THETA := atan2(DR,DC);
            THETAQ := quantize_angle(THETA);
            D := abs(C*cos(THETAQ) - R*sin(THETAQ));
            DQ := quantize_distance(D);
            A[DQ,THETAQ] := A[DQ,THETAQ] + GMAG;
            PTLIST(DQ, THETAQ) := append(PTLIST(DQ, THETAQ), [R, C])
                                                               Adapted from Shapiro and Stockman
```

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Algorithm 7: Hough Transform for Finding Straight Lines





- Extracting the line segments from the accumulators:
- 1. Pick the bin of A with highest value V
- 2. While V > value\_threshold {
  - 1. order the corresponding pointlist from PTLIST
  - 2. merge in high gradient neighbors within 10 degrees
  - 3. create line segment from final point list
  - 4. zero out that bin of A
  - 5. pick the bin of A with highest value V



(a) Infrared (b) Thresholded gradient image. (c) Hough transform. (d) Linked pixels. (Courtesy of Mr. D. R. Cate, Texas Instruments, Inc.)

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**FIGURE 10.34** (a) A 502  $\times$  564 aerial image of an airport. (b) Edge image obtained using Canny's algorithm. (c) Hough parameter space (the boxes highlight the points associated with long vertical lines). (d) Lines in the image plane corresponding to the points highlighted by the boxes). (e) Lines superimposed on the original image.

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- Main idea: The gradient vector at an edge pixel points the center of the circle.
- Circle equations:
  - $r = r_0 + d \sin(\theta)$

r<sub>0</sub>, c<sub>0</sub>, d are parameters

•  $c = c_0 + d \cos(\theta)$ 



Adapted from Linda Shapiro, U of Washington

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```
Accumulate the circles in gray-tone image S to accumulator A.
             S[\mathbf{R}, \mathbf{C}] is the input gray-tone image.
             NLINES is the number of rows in the image.
             NPIXELS is the number of pixels per row.
             A[R, C, RAD] is the accumulator array.
             R is the row index of the circle center.
             C is the column index of the circle center.
             BAD is the radius of the circle.
                   procedure accumulate_circles(S,A);
                   A := 0;
                   PTLIST := 0;
                   for R := 1 to NLINES
                     for C := 1 to NPIXELS
                        for each possible value RAD of radius
                          THETA := compute_theta(S.R,C,RAD);
                          R0 := R - RAD^*\cos(THETA);
                          C0 := C - RAD*sin(THETA);
                          A[R0,C0,RAD] := A[R0,C0,RAD]+1;
                          PTLIST(R0,C0,RAD) := append(PTLIST(R0,C0,RAD),[R,C])
                                                                           Adapted from Shapiro and Stockman
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```



Adapted from Shapiro and Stockman 57

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Fig. 4.7 Using the Hough technique for circular shapes. (a) Radiograph. (b) Window. (c) Accumulator array for r = 3. (d) Results of maxima detection.

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Adapted from Shapiro and Stockman 58

## Model fitting

- Mathematical models that fit data not only reveal important structure in the data, but also can provide efficient representations for further analysis.
- Mathematical models exist for lines, circles, cylinders, and many other shapes.
- We can use the method of least squares for determining the parameters of the best mathematical model fitting the observed data.





60

- Given a set of observed points  $\{(x_i, y_i), i = 1, \dots, n\}$ .
- A straight line can be modeled as a function with two parameters:

$$y = ax + b.$$

• To measure how well a model fits a set of *n* observations can be computed using the *least-squares error criteria*:

$$LSE = \sum_{i=1}^{n} (ax_i + b - y_i)^2$$

where  $ax_i + b - y_i$  is the algebraic distance.

• The best model is the model with the paramaters minimizing this criteria.

- For the model y = ax + b, the parameters that minimize LSE can be found by taking partial derivatives and solving for the unknowns.



vertical offsets CS 484, Spring 2010

• If we use the geometric distance where ax + by + c = 0and  $a^2 + b^2 = 1$ , the solution for  $[a \ b]^T$  is the eigenvector corresponding to the smallest eigenvalue of



and 
$$c = -a \sum_{i=1}^{n} x_i - b \sum_{i=1}^{n} y_i$$
.



perpendicular offsets

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#### Problems in fitting:

- Outliers
- Error definition (algebraic vs. geometric distance)
- Statistical interpretation of the error (hypothesis testing)
- Nonlinear optimization
- High dimensionality (of the data and/or the number of model parameters)
- Additional fit constraints

## Model fitting: ellipses

 Fitting a general conic represented by a second-order polynomial

$$ax^{2} + bxy + cy^{2} + dx + ey + f = 0$$

can be approached by minimizing the sum of squared algebraic distances.

 See Fitzgibbon *et al.* (PAMI 1999) for an algorithm that constrains the parameters so that the conic representation is forced to be an ellipse.

## Model fitting: ellipses

```
% x,y are vectors of coordinates
function a=fit_ellipse(x,y)
% Build design matrix
  D = [x.*x x.*y y.*y x y ones(size(x))];
% Build scatter matrix
  S = D'*D;
% Build 6x6 constraint matrix
  C(6,6)=0; C(1,3)=-2; C(2,2)=1; C(3,1)=-2;
% Solve generalised eigensystem
  [gevec, geval] = eig(S,C);
% Find the only negative eigenvalue
  [NegR, NegC] = find(geval<0 & ~isinf(geval));</pre>
% Get fitted parameters
  a = gevec(:,NegC);
```

Simple six-line Matlab implementation of the ellipse fitting method.

Adapted from Andrew Fitzgibbon, PAMI 1999

## Model fitting: ellipses



Adapted from Andrew Fitzgibbon, PAMI 1999

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Algorithm 15.1: Incremental line fitting by walking along a curve, fitting a line to runs of pixels along the curve, and breaking the curve when the residual is too large

Put all points on curve list, in order along the curve Empty the line point list Empty the line list Until there are too few points on the curve Transfer first few points on the curve to the line point list Fit line to line point list While fitted line is good enough Transfer the next point on the curve to the line point list and refit the line end Transfer last point(s) back to curve Refit line Attach line to line list end








## Model fitting: incremental line fitting



# Edge tracking

- Mask-based approach uses masks to identify the following events:
  - start of a new segment,
  - interior point continuing a segment,
  - end of a segment,
  - junction between multiple segments,
  - corner that breaks a segment into two.



# Edge tracking: ORT Toolkit

- Designed by Ata Etemadi.
- The algorithm is called Strider and is like a spider moving along pixel chains of an image, looking for junctions and corners.
- It identifies them by a measure of local asymmetry.
  - When it is moving along a straight or curved segment with no interruptions, its legs are symmetric about its body.
  - When it encounters an obstacle (i.e., a corner or junction) its legs are no longer symmetric.
  - If the obstacle is small (compared to the spider), it soon becomes symmetrical.
  - If the obstacle is large, it will take longer.
- The accuracy depends on the length of the spider and the size of its stride.
  - The larger they are, the less sensitive it becomes.

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# Edge tracking: ORT Toolkit

The measure of asymmetry is the angle between two line segments.

L1: the line segment from pixel 1 of the spider to pixel N-2 of the spider



L2: the line segment from pixel 1 of the spider to pixel N of the spider

The angle must be <= arctan(2/length(L2))

Longer spiders allow less of an angle.

Adapted from Linda Shapiro, U of Washington

angle 0

here

# Edge tracking: ORT Toolkit

- The parameters are the length of the spider and the number of pixels per step.
- These parameters can be changed to allow for less sensitivity, so that we get longer line segments.
- The algorithm has a final phase in which adjacent segments whose angle differs by less than a given threshold are joined.
- Advantages:
  - Works on pixel chains of arbitrary complexity.
  - Can be implemented in parallel.
  - No assumptions and parameters are well understood.

## Example: building detection



by Yi Li @ University of Washington

## Example: building detection





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Figure 5: A sample scale-map formation. CS 484, Spring 2010

Figure 9: State space for a given sub segment layout.

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NCL SS #2

NCL SS #3



# Figure 12: 3-scale simplification process over a natural image and the final CL segment extracted.

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Original	Proposed	КМСС	GBIS	JSEG	Original	Proposed	КМСС	GBIS	JSEG
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- Mauro Costa's dissertation at the University of Washington for recognizing 3D objects having planar, cylindrical, and threaded surfaces:
  - Detects edges from two intensity images.
  - From the edge image, finds a set of high-level features and their relationships.
  - Hypothesizes a 3D model using relational indexing.
  - Estimates the pose of the object using point pairs, line segment pairs, and ellipse/circle pairs.
  - Verifies the model after projecting to 2D.



(g) Image 7 (left)

(h) Image 8 (right)

(i) Image 9 (right)

Example scenes used. The labels "left" and "right" indicate the direction of the light source.

CS 484, Spring 2010





(e) Circular arc features detected

(f) Ellipses detected

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Figure 22: Sample run of the system.





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Figure 3: Relations between sample pairs of features.



- Learning phase: relational indexing by encoding each 2-graph and storing in a hash table.
- Matching phase: voting by each 2-graph observed in the image.



#### \_\_\_\_ Incorrect hypothesis









- 1. The matched features of the hypothesized object are used to determine its **pose**.
- 2. The **3D mesh** of the object is used to project all its features onto the image.
- 3. A **verification procedure** checks how well the object features line up with edges on the image.