

## Homework #4

Due November 8, 2012, beginning of the class

1. Answer the following questions regarding MD5 and SHA-1:
  - (a) Note that a message is still padded even if its length is already a multiple of the block length. Why is this important? I.e., what would the problem be if such messages are digested as they are without any padding?
  - (b) Discuss the relation between these hash functions and the Davies-Meyer construction based on a block cipher.
  - (c) Why do you think byte operations such as AND, OR, XOR are used instead of S-boxes in the nonlinear  $F$  function? What would happen if a structure like the DES  $F$  function were used instead of the current functions?
2. Compare the RSA and ElGamal signature schemes' performance in terms of
  - efficiency of the verification operation,
  - ability to pre-compute most of the signature operation in advance.

Which scheme should be preferred for an SSL certificate? Which scheme should be preferred for a real-time authentication protocol on a restricted device—e.g., an RFID tag on an electronic passport? Explain why.

3. Find the solution of the system

$$\begin{aligned}x &\equiv 3 \pmod{5} \\x &\equiv 2 \pmod{6} \\x &\equiv 1 \pmod{7}\end{aligned}$$

in  $\mathbb{Z}_{210}$ , using the Chinese Remainder Theorem and the extended Euclid's algorithm. Show all your work.

4. Question 4, the midterm exam of Fall 2010.